

AQA Qualifications

GCSE Mathematics

Unit 1: Higher 43601H Mark scheme

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Mark schemes are prepared by the Lead Assessment Writer and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation events which all associates participate in and is the scheme which was used by them in this examination. The standardisation process ensures that the mark scheme covers the students' responses to questions and that every associate understands and applies it in the same correct way. As preparation for standardisation each associate analyses a number of students' scripts: alternative answers not already covered by the mark scheme are discussed and legislated for. If, after the standardisation process, associates encounter unusual answers which have not been raised they are required to refer these to the Lead Assessment Writer.

It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of students' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.

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Glossary for Mark Schemes

GCSE examinations are marked in such a way as to award positive achievement wherever possible. Thus, for GCSE Mathematics papers, marks are awarded under various categories.

If a student uses a method which is not explicitly covered by the mark scheme the same principles of marking should be applied. Credit should be given to any valid methods. Examiners should seek advice from their senior examiner if in any doubt.

- M Method marks are awarded for a correct method which could lead to a correct answer.
- **M dep** A method mark dependent on a previous method mark being awarded.
- A Accuracy marks are awarded when following on from a correct method. It is not necessary to always see the method. This can be implied.
- **B** Marks awarded independent of method.
- **B dep** A mark that can only be awarded if a previous independent mark has been awarded.
- ft Follow through marks. Marks awarded following a mistake in an earlier step.
- **SC** Special case. Marks awarded within the scheme for a common misinterpretation which has some mathematical worth.
- **oe** Or equivalent. Accept answers that are equivalent. eg, accept 0.5 as well as $\frac{1}{2}$
- [*a*, *b*] Accept values between *a* and *b* inclusive.
- **[a, b)** Accept values $a \le value < b$
- **3.14...** Accept answers which begin 3.14 eg 3.14, 3.142, 3.1416

Examiners should consistently apply the following principles

Diagrams

Diagrams that have working on them should be treated like normal responses. If a diagram has been written on but the correct response is within the answer space, the work within the answer space should be marked. Working on diagrams that contradicts work within the answer space is not to be considered as choice but as working, and is not, therefore, penalised.

Responses which appear to come from incorrect methods

Whenever there is doubt as to whether a candidate has used an incorrect method to obtain an answer, as a general principle, the benefit of doubt must be given to the candidate. In cases where there is no doubt that the answer has come from incorrect working then the candidate should be penalised.

Questions which ask candidates to show working

Instructions on marking will be given but usually marks are not awarded to candidates who show no working.

Questions which do not ask candidates to show working

As a general principle, a correct response is awarded full marks.

Misread or miscopy

Candidates often copy values from a question incorrectly. If the examiner thinks that the candidate has made a genuine misread, then only the accuracy marks (A or B marks), up to a maximum of 2 marks are penalised. The method marks can still be awarded.

Further work

Once the correct answer has been seen, further working may be ignored unless it goes on to contradict the correct answer.

Choice

When a choice of answers and/or methods is given, mark each attempt. If both methods are valid then M marks can be awarded but any incorrect answer or method would result in marks being lost.

Work not replaced

Erased or crossed out work that is still legible should be marked.

Work replaced

Erased or crossed out work that has been replaced is not awarded marks.

Premature approximation

Rounding off too early can lead to inaccuracy in the final answer. This should be penalised by 1 mark unless instructed otherwise.

Continental notation

Accept a comma used instead of a decimal point (for example, in measurements or currency), provided that it is clear to the examiner that the candidate intended it to be a decimal point.

Q	Answer Mark Comments			
	Any two of the three valid criticisms ie the overlap the options not being exhaustive the lack of a time frame	B2	B1 Any one valid criticism eg If you had stayed in 3 which b tick? Some people might have stay than 14 Should say 'How many hotels stayed at in the last week/yea	red in more have you
	Ad			
	Do not accept the same criticism repeated eg 1 There is no box for 15 2 There is no box for 16			B1 B0
1(a)	Ignore irrelevant statements			
	Ignore criticisms of the question (other			
	The numbers collide $0 - 3$, $3 - 6$			B1
	No box for Other			B1
	No box for Don't know			B1
	There is a gap			B1
	They assume everyone has stayed in a hotel and it doesn't have an option for over 14 (ignore any non-contradictory statement)			B1
	There are not enough boxes			B0
	The boxes are wrong			B0

Q	Answer Mark Comments			
	Suitable response section covering 0 to 7, exhaustive, no overlaps, with at least 3 separate numerical choices	B1		
	Ad	ditional G	Guidance	
	Interpret box labelled eg 5+ in favour of the student			
	Ignore boxes that extend beyond 7 and 0 – 2, 3 – 5, 6 – 8 0 – 5, 6 – 10, 11 – 15	d do not co	ount them eg	B1 B0
1(b)	Ignore boxes labelled Other and Not su	ure etc		
	A box including 0 with another box labe	e (oe) is an overlap	B0	
	If inequalities are used they must be correct Allow tally table even if filled in			
	Boxes (oe) for 0 oe, 1, 2, 3, 4, 5, 6, 7		B1	
	Boxes (oe) for Mon, Tues, Wed, Thurs, Fri, Sat, Sun			В0

Q	Answer	Mark	Comments	
	Alternative method 1			
	36(%) or 0.36 or 64 : 36 or 32 : 18	M1	oe	
			Accept 1 : 0.5625 or 1 : $\frac{9}{16}$	
	16 : 9	A1	or 1.7 : 1 or 16 : 1	
			SC1 correctly simplifying any g	iven ratio
			SC1 for simplified ratio in reve	rse eg 9 : 16
	Alternative method 2			
2	$\frac{16}{25}$ or $\frac{9}{25}$ or $\frac{16}{9}$ or $\frac{9}{16}$	M1	Must be simplified fraction	
			Accept 1 : 0.5625 or 1 : $\frac{9}{16}$	
	16 : 9	A1	or 1.7:1 or 16 :1	
			SC1 correctly simplifying any g	jiven ratio
			SC1 for simplified ratio in rever	rse eg 9 : 16
	Additional Guidance			
	16 : 9 seen then answer 4 : 3			M1A0
	16% : 9%			M1A0

Q	Answer	Mark	Comments	
	Alternative method 1			
	360 – 165 – 60 or 135	M1	Angle for cows May be on diagram	
	their 135 ÷ 360 (× 100) or 0.375	M1dep	oe Proportion of cows	
	37.5	A1	Accept 38 with method	
	Alternative method 2			
3	60 ÷ 360 (× 100) or 0.166(6) or 16.6(6) (%) and 165 ÷ 360 (× 100) or 0.458(3) or 45.8(3) (%)	M1	Proportions of chickens and sh oe May be on diagram	leep
	or (60 + 165) ÷ 360 or 0.625 (1 – their 0.1666 – their 0.4583) (× 100) or		Proportion of cows	
	their 16.66 + their 45.83 or	M1dep	oe	
	(60 + 165) ÷ 360 × 100 or 62.5 (%)		Percentage of chickens and sh	eep
	37.5	A1	Accept 38 with method	
	Additional Guidance			
	0.625			M1
	62.5 or 0.375			M1M1
	Accuracy lost through truncation or rou	undina is o	nly penalised in the final mark	

Q	Answer	Mark	Comments
4(a)	Positive	B1	Ignore any indication of strength eg weak
4(b)	7	B1	Accept any answer in range [6.8, 7.2]

	Appropriate key	B1		
	Stem 2, 3, 4, 5	B1	or 5, 4, 3, 2	
	Leaves correct and ordered 1 4 9 2 5 6 8 8 9 0 3 7 8 2 6	B1	Must match the order of their stem if present eg if 5, 4, 3, 2 leaves should be 6 2 8 7 3 0 9 8 8 6 5 2 9 4 1	
5(a)	Appropriate alignment of leaves	Q1ft	ft their single digit leaves Strand (ii) Logical organised working so row lengths show the distribution	
	Additional Guidance			
	 For the Q mark: Leaves may be unordered and/or incorrect (but need at least 13) Leaves must be single digit Lengths of rows need to correspond to <i>their</i> number of leaves ie row with most leaves should be longest etc 			
	The Q mark is independent so B0B0B0Q1ft is possible			
	Ignore eg lines between numbers which may be working for 5b and commas			
	If not crossed out and replaced, mark the stem-and-leaf on the grid			

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	Alternative method 1				
	11 × 10 or 110 or 2 × 20 or 40	M1	oe Implied by 4.40 or 440 or 1.60) or 160	
	(their 110 + their 40) × 0.04 or (their 110 + their 40) × 4 or 600	M1dep	oe		
	6	A1			
5(b)	Alternative method 2				
	10 × 0.04 or 0.4 or 10 × 4 or 40 or 20 × 0.04 or 0.8 or 20 × 4 or 80	M1	oe Allow 30 × 4 or 1.20 or 120 fo	r M1 only	
	their 0.4 × 11 + their 0.8 × 2 M1dep oe or M1dep oe their 40 × 11 + their 80 × 2 or 600 M1dep oe				
	6	A1			
	Additional Guidance				
	(Total points =) 150 scores the first mark			M1	
	$13 \times 10 + 2 \times 20 = 170$ $170 \times 4 = 680$ £6.80			M1 M1dep A0	

Q	Answer	Mark	Comments	
	4 or 5 correct plots	M1	(25, 5), (35, 13), (45, 9), (55, 6) $\pm \frac{1}{2}$ small square Accept 5 points plotted at the consistently on the lower upper bound for M1 only	prrect
	5 correct plots joined with straight lines to form a frequency polygon	A1	$\pm \frac{1}{2}$ small square	
6	Additional Guidance			
	Accept unruled lines if intention for stra	aight lines	is clear	M1A1
	Bar chart and frequency polygon drawn – mark frequency polygon			
	Bar chart only			MO
	Ignore other points or lines before first first and last plot	plot and a	fter final plot and a line joining	

	$\frac{3}{25}$ × 100 or 12	M1	oe Allow $\frac{12}{100}$ or 12%	
	$\frac{1}{10}$ × (100 – 20) or 8	M1	oe Allow <mark>8</mark> 80	
7	4	A1		
	Additional Guidance			
	$(\frac{3}{25} - \frac{1}{10}) \times 100$		M1 M0 A0	0
	$(\frac{3}{25} - \frac{1}{10}) \times 80$		M0 M1 A0	0

Q	Answer	Mark	Comments
		I	
8(a)	24	B1	
		-	
	F(45) = [71, 73] or F(44) = [70, 72] or F(37) = [57, 59] or F(36) = [55, 57] or F(>45) = [7, 9] or F(>44) = [8, 10] or F(>37) = [21, 23] or F(>36) = [23, 25]	M1	
8(b)	F(45) = [71, 73] or F(44) = [70, 72] and F(37) = [57, 59] or F(36) = [55, 57] or F(>45) = [7, 9] or F(>44) = [8, 10] and F(>37) = [21, 23] or F(>36) = [23, 25]	M1dep	
	[12, 17]	A1	
	Ad	Guidance	
	Answer only in range		M1M1A1
	Answer in range from wrong working		M2 max

Q Answer Mar	Comments
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	Upper quartile drawn at 41	B1	$(\pm \frac{1}{2}$ square)			
	Upper quartile and lower quartile drawn with interquartile range of 20	B1ft	$(\pm \frac{1}{2}$ square) ft their upper quartile – 20			
	$44 \times \frac{3}{4}$	$44 \times \frac{3}{4}$ M1 eg 44 : 33 seen in working				
	Median at 33	A1	(± ¹ / ₂ square) NB Must have a fully correct diagram for all 4 marks			
9	Additional Guidance					
	Line drawn at 33 (not LQ or UQ)	M1A1				
	Box with two medians can still score Lo	B1B1M0A0 possible				
	Instructions for incomplete diagrams:					
	 If a line at 33 is shown can imply this is their median If three lines are drawn assume LQ, median, UQ, even without box For the following: 					
	implies LQ					
	implies UQ					
	implies LQ and U	Q				

Q	Answer	Mark	Comments	
	Selects 4.2×10^{-4} and 0.005	B1	oe 0.00042 5 × 10 $^{-3}$ May be implied by 0.0027(1) oe	
10(a)	Finds the midpoint of any two of the numbers eg $(4.2 \times 10^{-4} + 0.005) \div 2$ or $0.0027(1)$	M1	Allow an incorrect number of leading zeros if numbers converted incorrectly 0.000 245 or 0.002 535 or 0.003 235 or 0.003 41 or 0.005 7 all imply B0M1 oe	
	2.7(1) × 10 ^{−3}	Q1ft	Strand (i) ft B0M1 for correct midpoint of two of the numbers, given in standard form SC2 2.45×10^{-4} or 2.535×10^{-3} or 3.235×10^{-3} or 3.41×10^{-3} or 5.7×10^{-3}	
	Additional Guidance			

10(b)	stays the same	B1	
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Q	Answer	Mark	Comments	
	Selects at least two (and no others) from Centre (and miss) or miss and centre or outer and outer	B1	Seen or implied eg At least two pairs selected from 0.2 (and 0.3) 0.3 and 0.2 0.5 and 0.5 (and no others) Allow outer-outer repeated as a fourth pair	
	0.2 × 0.3 (× 2) or 0.06 or 0.12 or 0.5 × 0.5 or 0.25	M1	oe Allow other combinations seen	
11	0.2 × 0.3 (× 2) or 0.06 or 0.12 and 0.5 × 0.5 or 0.25	M1	oe No other combinations used	
	0.37	A1	oe fraction, decimal or percentage SC3 for 0.31 (ignoring reverse) SC3 for 0.51 (assumes one dart allowed) SC2 for 0.61 (for total of 50+) SC2 for 0.62 (outer-outer twice) SC1 for 0.45 (50+ with order ignored)	
	Additional Guidance			

Q		Answe	r		Mark		Comr	nents
						B1 for any	one correct	entry
	2550	850	1400					-
	383	127	210			2550	850	1400
	or		1	B2	382 or 382.5	128 or 127.5	210	
12	2550	850	1400		or 383	or 127		
	382	128	210					
				Ad	ditional G	uidance		
				Ad	ditional G	uidance		

Q	Answer	Mark	Comments			
	Alternative method 1					
	Attempt at frequency density 300 ÷ 30 or 10 or 200 ÷ 10 or 20 or 260 ÷ 20 or 13 or 80 ÷ 40 or 2	M1	One frequency ÷ one class width			
	4 correct frequency densities	A1	10, 20, 13, 2			
	Widths correct and bars in correct positions	A1	Must have correct frequency density for at least two bars			
	Bars to correct heights and vertical A1 f	Δ1 ft	ft their frequency densities with M1 awarded			
			$\pm \frac{1}{2}$ small square			
13(a)	Alternative method 2					
	Attempt at standard frequencies eg 300 ÷ 3, 200 ÷ 1, 260 ÷ 2, 80 ÷ 4	M1	Any two attempted			
	4 correct standard frequencies	A1	eg 100, 200, 130, 20			
	Widths correct and bars in correct positions	A1	Must have correct standard frequency for at least two bars			
	Bars to correct heights and key	A1 ft	ft their standard frequencies with M1 awarded			
		,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,	$\pm \frac{1}{2}$ small square			
	Additional Guidance					
	Accept any scale that fits					
	eg 1 cm ≡ 2.5, 1 cm ≡ 3, 1 cm ≡ 4, 1 cm ≡ 5, 1 cm ≡ 10					

Q	Answer	Mark	Comments		
13(b)	$\frac{3}{4} \times 840$ or 630 or $\frac{1}{4} \times 840$ or 210	M1	oe		
	110	A1			
	Additional Guidance				

Q	Answer	Mark	Comments			
	Alternative method 1					
	$\frac{9}{15} \times \frac{x}{14}$ or $\frac{3}{15} \times \frac{x}{14}$	M1	oe			
	$\frac{9}{15} \times \frac{6}{14}$ or $\frac{54}{210}$ or $\frac{9}{35}$		P(R, R')			
	or $\frac{9}{15} \times \frac{3}{14}$ or $\frac{27}{210}$ or $\frac{9}{70}$		P(R, Y) or P(R, G)			
	or $\frac{3}{15} \times \frac{12}{14}$ or $\frac{36}{210}$ or $\frac{6}{35}$	M1dep	P(Y, Y') or P(G, G')			
	or $\frac{3}{15} \times \frac{9}{14}$ or $\frac{27}{210}$ or $\frac{9}{70}$		P(Y, R) or P(G, R)			
14	or $\frac{3}{15} \times \frac{3}{14}$ or $\frac{9}{210}$ or $\frac{3}{70}$		P(Y, G) or P(G, Y)			
			oe 0.257(142) or 0.128(571) or 0.171(428) or 0.042(857)			
	$\frac{9}{15} \times \frac{6}{14} + \frac{3}{15} \times \frac{12}{14} + \frac{3}{15} \times \frac{12}{14}$		oe $\frac{54}{210} + \frac{36}{210} + \frac{36}{210}$			
	or	M1dep	or			
	$\frac{9}{15} \times \frac{3}{14} \times 2 + \left(\frac{3}{15} \times \frac{9}{14} + \frac{3}{15} \times \frac{3}{14}\right) \times 2$		$\frac{27}{210} \times 2 + \left(\frac{27}{210} + \frac{9}{210}\right) \times 2$			
	$\frac{126}{210}$ or $\frac{3}{5}$ or 0.6	A1	oe SC2 for $\frac{126}{225}$ or $\frac{14}{25}$ oe			

Q	Answer	Mark	Comments	
	Alternative method 2	<u> </u>		
	$\frac{9}{15} \times \frac{x}{14}$ or $\frac{3}{15} \times \frac{x}{14}$	M1	ое	
	$\frac{9}{15} \times \frac{8}{14}$ or $\frac{72}{210}$ or $\frac{12}{35}$		P(R, R)	
14	or $\frac{3}{15} \times \frac{2}{14}$ or $\frac{6}{210}$ or $\frac{1}{35}$	M1dep	P(Y, Y) or P(G, G) oe 0.342(857) or 0.028(571)	
cont.	$1 - (\frac{9}{15} \times \frac{8}{14} + \frac{3}{15} \times \frac{2}{14} + \frac{3}{15} \times \frac{2}{14})$	M1dep	oe $1 - (\frac{72}{210} + \frac{6}{210} + \frac{6}{210})$	
	$\frac{126}{210}$ or $\frac{3}{5}$ or 0.6	A1	oe SC2 $\frac{141}{225}$ or $\frac{47}{75}$ oe	
	Additional Guidance			
	Probabilities combined on a tree diagram			M1M1
	Note that P(R) = 0.6			

Q	Answer	Mark	Comments
	Alternative method 1		
	455 or 465 or 505 or 515 seen	B1	May be implied by 960 or 980
	their 455 + their 505 or 960	M1	their 455 must be [450, 460) their 505 must be [500, 510)
	26 000 ÷ (455 + 505) or 26 000 ÷ 960 or 27.0833	M1	Allow 26 005
	27	A1	Must be using 26 000 and 960 SC2 26 from 26 000 ÷ 980
	Alternative method 2		
15	455 or 465 or 505 or 515 seen	B1	May be implied by 960 or 980
	their 455 + their 505 or 960	M1	their 455 must be [450, 460) their 505 must be [500, 510)
	(455 + 505) × 27 = 25 920 and (455 + 505) × 28 = 26 880 or 960 × 27 = 25 920 and 960 × 28 = 26 880	M1	
	27	A1	Must be using (26 000 and) 960 SC2 26 from 26 000 ÷ 980
	Additional Guidance		